## Chapter-27

Coordination Chemistry: Crystal Field Stabilization Energy (CFSE)<br>Arijit Das<br>Department of Chemistry, Bir Bikram Memorial College, Agartala, Tripura, India<br>Email: arijitdas78chem@gmail.com

The crystal field stabilization energy (CFSE) is defined as the stability achieved by placing a transition metal ion in the crystal field originated by a group of ligands arranged in a particular symmetry. It is the result of splitting of the d orbitals in the ligand field. Some of the orbitals become higher and some lower in energy after splitting. The electrons occupying the lower set of orbitals result in the stabilization of the central metal ion of the coordination complex by the amount of energy called crystal field stabilization energy.

The CFSE will depend on multiple factors including geometry of the coordination compounds (which changes the d-orbital splitting patterns), number of d-electrons, spin pairing energy, crystal field splitting energy ( $\Delta$ ) and strength of ligand (Spectrochemical series).

Spectrochemical series: Increasing order of strength of ligands:

$$
\mathbf{I}^{-}<\mathrm{Br}^{-}<\mathbf{C l}^{-}<\mathbf{S C N}^{-}<\mathbf{F}^{-}<\mathbf{O H}^{-}<\mathbf{C}_{2} \mathbf{O}_{4}{ }^{2-}<\mathbf{H}_{2} \mathbf{O}<\mathbf{N C S}^{-}<\mathbf{E D T A}^{4-}<\mathbf{N H}_{3}<\mathrm{en}<\mathbf{C N}^{-}<\mathbf{C O}
$$

## Derivation of Crystal Field Stabilization Energy (CFSE) in terms of $\Delta_{0}$ and Dq for Octahedral Geometry:

Let us consider a $\mathbf{d}^{\mathbf{p + q}}$ ion with $p$ electrons in $\mathrm{t}_{2 \mathrm{~g}}$ and q electrons in $\mathrm{e}_{\mathrm{g}}$ orbitals, then from the CFT splitting diagram we can write,

Gain in energy due to $\mathbf{q}$ electrons in $\mathbf{e}_{\mathrm{g}}$ orbitals (in terms of $\Delta_{\mathbf{o}}$ ) $=+\mathbf{0 . 6} \Delta_{\mathbf{0}} \mathbf{x ~} \mathbf{q}$ and loss in energy due to $\mathbf{p}$ electrons in $\mathbf{t}_{2 g}$ orbitals (in terms of $\Delta_{0}$ ) $=\mathbf{- 0 . 4} \Delta_{0} \mathbf{x} \mathbf{p}$

Thus net change in energy in terms of $\Delta_{0}$ will be given for $d^{p+q}$ ion

$$
\begin{equation*}
=[-0.4 p+0.6 q] \Delta_{\mathrm{q}} \tag{1}
\end{equation*}
$$

Since, $\Delta_{0}=10 \mathrm{Dq}$, thus change in energy in terms of Dq for $\mathrm{d}^{\mathrm{p}+\mathrm{q}}$ ion $=[-4 p+6 q] D q$
If P be the mean pairing energy which is the energy required to pair two electrons against electron-electron repulsion in the same orbital and $m=$ number of electron pairs, then for octahedral complexes

$$
\text { CFSE }=[-0.4 p+0.6 q] \Delta_{0}+\mathbf{m P}------(3)
$$

## Derivation of Crystal Field Stabilization Energy <br> (CFSE) in terms of $\Delta_{t}$ for Tetrahedral Geometry:

Let us consider a $\mathrm{d}^{\mathrm{p}+\mathrm{q}}$ ion with p electrons in $\mathrm{t}_{2 \mathrm{~g}}$ and q electrons in $\mathrm{e}_{\mathrm{g}}$ orbitals, then from the CFT splitting diagram we can write,
Loss in energy due to $q$ electrons in $\mathbf{e}_{\mathrm{g}}$ orbitals (in terms of $\Delta_{\mathfrak{t}}$ ) $=\quad \mathbf{- 0 . 6} \Delta_{\mathrm{t}} \mathbf{x} \mathbf{q}$ and gain in energy due to $\mathbf{p}$ electrons in $\mathbf{t}_{\mathbf{2 g}}$ orbitals (in terms of $\Delta_{t}$ ) $=0.4 \Delta_{t} \mathbf{x} \mathbf{p}$

Thus net change in energy in terms of $\Delta_{t}$ will be given for $d^{p+q}$ ion

$$
=[0.4 p-0.6 q] \Delta_{t} \cdots \cdots-\cdots-\cdots(4)
$$

If P be the mean pairing energy which is the energy required to pair two electrons against electron-electron repulsion in the same orbital and $m=$ number of electron pairs, then, for Tetrahedral complexes

$$
\begin{equation*}
\text { CFSE }=[0.4 p-0.6 q] \Delta_{t}+m P \tag{5}
\end{equation*}
$$

## Crystal Field Stabilization Energy

(CFSE) in terms of $\Delta_{t}, \Delta_{0}$ and $\mathbf{D}_{q}$ for tetrahedral geometry

For $\mathrm{d}^{\mathrm{p}+\mathrm{q}}$ ion of tetrahedral complexes with p electrons in $\mathrm{t}_{2 \mathrm{~g}}$ and q electrons in $\mathrm{e}_{\mathrm{g}}$ orbitals,

$$
\begin{aligned}
& \text { CFSE }=[-0.6 q+0.4 p] \Delta_{t}+m P------(6)\left(i n ~ t e r m s ~ o f ~ \Delta_{t}\right) \\
& \left.=[-0.6 q+0.4 p](4 / 9) \Delta_{0}+m P----- \text { (7) (in terms of } \Delta_{0}\right)
\end{aligned}
$$

[Here, $\mathrm{m}=$ number of electron pair and $\mathrm{P}=$ Mean pairing energy, which is the energy required to pair two electrons against electron-electron repulsion in the same orbital]
$\Delta_{\text {tet }}$ is approximately $4 / 9 \Delta_{0}$
$\Delta_{\text {tet }}$ is approximately $\left.\mathbf{4 0 / 9} \mathbf{~ D q ~ ( 1 ~} \Delta_{\mathbf{0}}=10 \mathrm{Dq}\right)$
Calculation of difference in CFSE value for Octahedral \& Tetrahedral $3 \mathbf{d}^{\mathbf{3}}(\mathbf{H S})$ complexes

- For a HS d ${ }^{\mathbf{3}}\left(\mathbf{E} . C .-\mathbf{t}_{\mathbf{2 g}}{ }^{\mathbf{3}}, \mathbf{e}_{\mathbf{g}}{ }^{\mathbf{0}}\right)$ octahedral complexes, the Crystal Field Stabilization Energy $=[-0.4 \mathrm{p}+0.6 \mathrm{q}] \times \Delta_{\mathrm{o}}+\mathrm{mP}=-(3 \times 0.4) \Delta \mathrm{o}=\mathbf{- 1 . 2 \Delta o}---\mathbf{( 1 )}$

For a HS d ${ }^{\mathbf{3}}\left(\mathbf{E}\right.$. C. $\left.^{-}-\mathbf{t}_{\mathbf{2 g}}{ }^{1}, \mathbf{e}_{\mathrm{g}}{ }^{2}\right)$ tetrahedral complexes, the

$$
C F S E=[-\mathbf{0 . 6 q}+\mathbf{0 . 4 p}] \times \Delta_{\mathbf{t}}+\mathbf{m P}=[-\mathbf{0 . 6} \mathbf{x} \mathbf{2}+\mathbf{0 . 4} \mathbf{x} \mathbf{1}] \times \Delta_{\mathbf{t}}=-\mathbf{0 . 8} \mathbf{A}_{\mathbf{t}}
$$

- Now use the relation $\Delta_{t}=4 / 9 \Delta_{\mathbf{o}}$
- So for tetrahedral d ${ }^{3}$ HS, the Crystal Field Stabilization Energy CFSE

$$
=-0.8 \times 4 / 9 \Delta_{0}=-0.355 \Delta_{0}----(2)
$$

- And the difference in Crystal Field Stabilization Energy (CFSE) between the two geometries will be: Eq. 1 - Eq. $2=(1.2-0.355) \underline{\Delta}_{0}=0.845 \underline{\Delta}_{0}$
(N.B.: Ignore negative signs of CFSE to predict the difference between CFSE value of two geometries).

Table-1: CFSE Value in terms of $\Delta_{0}$ and $\Delta_{t}$ for HS 3d ${ }^{\mathbf{0}}$ to $\mathbf{3 d}{ }^{10}$ Octahedral and Tetrahedral complexes


Table-2: CFSE Value in terms of $\Delta_{0}$ and $\Delta_{t}$ for LS 3d ${ }^{\mathbf{0}}$ to $\mathbf{3 d}{ }^{10}$ Octahedral and Tetrahedral complexes


Table 3: Comparative study for Crystal Field Stabilization Energies (CFSE) for octahedral and tetrahedral geometries, assuming high spin (HS) configurations.

The units are $\Delta_{0}$, and assuming that $\Delta_{\text {tet }}=4 / 9 \Delta_{0}$

| $3 \mathrm{~d}^{\mathrm{n}}$ | Octahedral | Tetrahedral | Difference |
| :---: | :---: | :---: | :---: |
| $3 \mathrm{~d}^{0}, \mathrm{~d}^{5}, \mathrm{~d}^{10}$ | 0 | 0 | 0 |
| $3 \mathrm{~d}^{1}, \mathrm{~d}^{6}$ | 0.4 | 0.27 | 0.13 |
| $3 \mathrm{~d}^{2}, \mathrm{~d}^{7}$ | 0.8 | 0.53 | 0.27 |

## Related Questions

Q.1. The electronic spectrum of $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right]^{3+}$ shows a single broad peak with a maximum at $20,300 \mathrm{~cm}^{-1}$. The crystal field stabilization energy (CFSE) of the complex ion, in $\mathrm{kJ} \mathrm{mol}^{-1}$, is ( $1 \mathrm{~kJ} \mathrm{~mol}^{-1}=83.7 \mathrm{~cm}^{-1}$ )
(a) 145.5
(b) 242.5
(c) 83.7
(d) 97
$\rightarrow$ Ans. (d)
In $\left[\mathrm{Ti}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{3+}, \mathrm{Ti}^{3+}$ ion of $d^{1}$ configuration is present in the octahedral complex. Under octahedral crystal field, the configuration of $\mathrm{Ti}^{3+}$ will be, $t_{2 g}^{1} e_{g}^{0}$.
So, $\quad$ CFSE $=[(-0.4) \times 1+(+0.6) \times 0] \Delta_{0}$

$$
\begin{aligned}
&=-0.4 \times \Delta_{0}=-0.4 \times 20,300 \mathrm{~cm}^{-1} \\
&= \quad\left[\because \Delta_{0}=20,300 \mathrm{~cm}^{-1}\right] \\
&=-0.4 \times \frac{20,300}{83,7} \mathrm{~kJ} \mathrm{~mol}^{-1} \\
&= {\left[\because=1 \mathrm{~kJ} \mathrm{~mol}^{-1}=83.7 \mathrm{~cm}^{-1}\right] } \\
& \Rightarrow \mathrm{CFSE}=97 \mathrm{~kJ} \mathrm{~mol}^{-1}
\end{aligned}
$$

Q.2. The crystal field stabilization energy (CFSE) of $\left[\mathrm{CoF}_{3}\left(\mathrm{H}_{2} \mathrm{O}\right)_{3}\right]\left(\Delta_{0}<\mathrm{P}\right)$ is
(a) $-0.8 \Delta_{0}$
(b) $-0.8 \Delta_{0}+2 P$
(c) $-0.4 \Delta_{0}$
(d) $-0.4 \Delta_{0}+P$
$\rightarrow$ Ans. (c)
$\left[\mathrm{CoF}_{3}\left(\mathrm{H}_{2} \mathrm{O}\right)_{3}\right]$ is an octahedral complex.
In this complex (compound) all ligands are weak field ligand. For weak field ligands $\Delta_{0}<P$ (pairing energy), so the electronic configuration of Co (III) will be $t_{2 g}^{4} e_{g}^{2}$.


Here, CFSE can be calculated as:

$$
\mathrm{CFSE}=[-0.4 p+0.6 q] \Delta_{0}
$$

Where, $\Delta_{0}=$ crystal field splitting energy in octahedral complex
$\mathrm{p}=$ Number of electrons in $\mathrm{t}_{2 g}$ orbitals $=4 \& \mathrm{q}=$ Number of electrons in $\mathrm{e}_{g}$ orbitals $=2$

$$
\text { Hence CFSE }=[-0.4 \times 4+0.6 \times 2] \Delta_{0}
$$

$$
=[-1.6+1.2] \Delta_{0}=\left[-0.4 \Delta_{0}\right]
$$

Hence, the crystal field stabilization energy (CFSE) of $\left[\mathrm{CoF}_{3}\left(\mathrm{H}_{2} \mathrm{O}\right)_{3}\right]$ will be $-0.4 \Delta_{0}$.
Q.3. The values of the crystal field stabilization energies for a high spin $\boldsymbol{d}^{6}$ metal ion in octahedral and tetrahedral fields respectively, are
(a) -0.4 $\Delta_{0}$ and -0.27 $\Delta_{t}$
(b) -1.6 $\Delta_{0}$ and $-0.4 \Delta_{t}$
(c) $\mathbf{- 2 . 4} \Delta_{0}$ and $\mathbf{- 0 . 6} \Delta_{t}$
(d) $-\mathbf{0 . 4} \Delta_{0}$ and $-0.6 \Delta_{t}$
$\rightarrow$ Ans. (d)
Crystal field stabilization energy (CFSE) for high spin $d^{6}$ metal ion.
Crystal field splitting in octahedral field.


CFSE $=\left[-0.4 n_{t 2 g}+0.6 n_{e_{g}}\right] \Delta_{0}$

$$
=[-0.4 \times 4+0.6 \times 2] \Delta_{0}=-0.4 \Delta_{0}
$$

Crystal field splitting in tetrahedral field


CFSE $=\left(-0.6 n_{e_{g}}+0.4 n_{t_{2 g}}\right) \Delta_{\mathrm{t}}$

$$
\begin{aligned}
& =(-0.6 \times 3+0.4 \times 3) \Delta_{\mathrm{t}} \\
& =(-1.8+1.2) \Delta_{\mathrm{t}}=-0.6 \Delta_{\mathrm{t}}
\end{aligned}
$$

Here, $\boldsymbol{n}_{\boldsymbol{t}_{2 g}}=$ number of electrons in $\mathbf{t}_{\mathbf{2 g}}$ and $\boldsymbol{n}_{\boldsymbol{e}_{g}}=$ number of electrons in $\mathbf{e}_{\mathrm{g}}$.
Q.4. The spin-only magnetic moment and crystal field stabilization energy [CFSE] of $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{3-}$ respectively, are [Note : lgnore the pairing energy]
a) $\mathbf{1 . 7 3} \mathrm{BM}$ and $\mathbf{- 2 . 0} \Delta_{0}$
b) 2.84 BM and $-1.6 \Delta_{0}$
c) 0 BM and $-2.4 \Delta_{0}$
d) 5.92 BM and 0
$\rightarrow$ Ans. (a)
In $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{-3}$, oxidation state of iron in $\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]^{-3}$ is $(+3)$. E.C. $\mathrm{Fe}^{3+}=3 \mathrm{~d}^{5}$.
It forms a low spin complex ( $\mathrm{CN}^{-}$is a strong field ligand).

$\therefore$ Number of unpaired electrons $(n)=1$
Spin only magnetic moment
$\mu_{\mathrm{s}}=\sqrt{n(n+2)} \mathrm{BM}=\sqrt{3}=1.73 \mathrm{BM}$
CFSE $=\left(\right.$ Number of electrons in $\left.\mathrm{t}_{2 g} \times-0.4 \Delta_{0}\right)+\left(\right.$ Number of electrons' in $\left.\mathrm{e}_{g} \times 0.6 \Delta_{0}\right)$.
$=(5 \times-0.4) \Delta_{0}=-2.0 \Delta_{0}$.
Q.5. The correct order of the spin only magnetic moments of the following complexes is
(I) $\left[\mathrm{Cr}\left(\mathrm{H}_{2} \mathrm{O}\right)_{6}\right] \mathrm{Br}_{2}$
(II) $\mathrm{Na}_{4}\left[\mathrm{Fe}(\mathrm{CN})_{6}\right]$
(III) $\mathrm{Na}_{3}\left[\mathrm{Fe}\left(\mathrm{C}_{2} \mathrm{O}_{4}\right)_{3}\right]\left(\Delta_{0}>\right.$ P)
(IV) $\left(\mathrm{Et}_{4} \mathrm{~N}\right)_{2}\left[\mathrm{CoCl}_{4}\right]$
a) (II) $\approx$ (I) $>$ (IV) $>$ (III)
b) (I) $>$ (IV) $>$ (III) $>$ (II)
c) (III) $>$ (I) $>$ (IV) $>$ (II)
d) (III) $>$ (I) $>$ (II) $>$ (IV)
$\rightarrow$ Ans. (b)
I. $\mathbf{I n}\left[\mathbf{C r}\left(\mathbf{H}_{2} \mathbf{O}\right)_{6}\right] \mathbf{B r}_{2}$, chromium is in $\mathrm{Cr}^{2+}$ having electronic configuration $[\mathrm{Ar}] 3 \mathrm{~d}^{4}$.
$\mathrm{H}_{2} \mathrm{O}$ is a weak field ligand.
It has octahedral geometry
$\therefore \quad 3 d^{4}=t_{2 g}^{3} e_{g}^{1}$
Unpaired electrons $=4$

$$
\begin{aligned}
\mu_{\mathrm{s}} & =\sqrt{4 \times 6} \\
& =\sqrt{24} \mathrm{BM} .
\end{aligned}
$$

II. $\mathbf{N a}{ }_{4}\left[\mathrm{Fe}(\mathbf{C N})_{6}\right] \rightarrow \mathrm{Fe}^{2+}=[\mathrm{Ar}] 3 \mathrm{~d}^{6}$
$\mathrm{CN}^{-}$is a strong field ligand
Octahedral geometry
$\therefore \quad 3 d^{6}=t_{2 g}^{6} e_{g}^{0}$
Unpaired electrons $=0$
$\mu_{\mathrm{s}}=0$
III. $\mathbf{N a}_{3}\left[\mathbf{F e}\left(\mathbf{C}_{2} \mathbf{O}_{4}\right)_{3}\right] \rightarrow \mathrm{Fe}^{3+}=[\mathrm{Ar}] 3 d^{5}$
$\Delta_{0}>p$ (Given), that is oxalate $\left(\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}\right)$ treated as stronger ligand.
Octahedral geometry
$\therefore \quad 3 d^{5}=t_{2 g}^{5} e_{g}^{0}$
Unpaired electrons $=1 ; \boldsymbol{\mu}_{\mathrm{s}}=\sqrt{\mathbf{3}}=\mathbf{1 . 7 3} \mathbf{B M}$
IV. $\left(\mathbf{E t}_{4} \mathrm{~N}_{2}\right)_{2}\left[\mathrm{CoCl}_{4}\right]^{2-} ; \mathrm{Co}^{2+}=[\mathrm{Ar}] 3 \mathrm{~d}^{7}$
$\mathrm{Cl}^{-}$is a weak field ligand.
In this complex, coordination number is 4
Tetrahedral geometry
Splitting of $d$ - orbitals in tetrahedral field is


Unpaired electrons $=3$

$$
\boldsymbol{\mu}_{\mathrm{s}}=\sqrt{\mathbf{1 5}} \mathbf{B M}
$$

$\therefore$ Spin only magnetic moment order is I $>$ IV $>$ III $>$ II
Q.6. The complex ion that will lose its crystal field stabilization energy upon oxidation of its metal to +3 state is (ignore pairing energy)

a) $\left[\mathrm{Co}(\mathrm{phen})_{3}\right]^{2+}$
b) $\left[\mathrm{Ni}(\mathrm{phen})_{3}\right]^{2+}$
c) $\left[\mathrm{Zn}(\text { phen })_{3}\right]^{2+}$
d) $\left[\mathrm{Fe}(\mathrm{phen})_{3}\right]^{2+}$
$\rightarrow$ Ans. (d)
The complex ion that will lose its crystal field stabilization energy upon oxidation of its metal to +3 state is $\left[\mathrm{Fe}(\text { phen })_{3}\right]^{2+}$.


In $\left[\mathrm{Fe}(\text { phen })_{3}\right]^{2+}$, electronic configuration of $\mathrm{Fe}^{2+}$ is $3 d^{6} 4 s^{0}$. Phenanthrene is a strong field symmetrical bidentate ligand. The E.C. of $\mathbf{F e}^{2+}$ is as follows:


$$
\text { CFSE }=6 \times-0.4 \Delta_{0}=-2.4 \Delta_{0} .
$$

The splitting of orbital and arrangement of electrons (E.C.) in $\mathrm{Fe}^{3+}$ is as follows:

$\mathrm{Fe}^{2+}$ upon oxidation of its metal to (+3) state lose its CFSE from -2.4 $\Delta_{0}$ to - $2.0 \Delta_{0}$.

## Reference Books:

1. Introduction to Coordination Chemistry, Geoffrey A. Lawrance
2. Coordination Chemistry, Joan Ribas Gispert
3. Coordination Chemistry, 20: Invited Lectures Presented at the 20th International Conference on Coordination Chemistry, Calcutta, India, 10-14 December 1979, D. Banerjea
4. Comprehensive Coordination Chemistry III, Gerard Parkin, Edwin C Constable, Lawrence Que Jr.
